

# Groups and Rings (11)

## Example of a subgroup lattice

$$C_{12} = \langle x \rangle = \langle x^1 \rangle. \text{ Divisor of } 12 : 1, 2, 3, 4, 6, 12$$

$$\langle x^2 \rangle = \{x^2, x^4, x^6, x^8, x^{10}, x^{12} = e\}$$

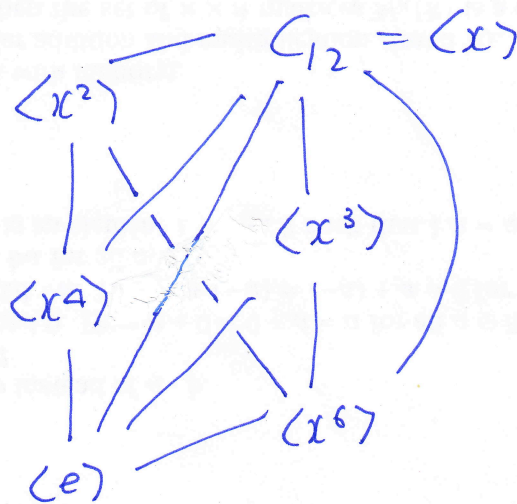
$$\langle x^3 \rangle = \{x^3, x^6, x^9, x^{12} = e\}$$

$$\langle x^4 \rangle = \{x^4, x^8, x^{12} = e\}$$

$$\langle x^6 \rangle = \{x^6, x^{12} = e\}$$

$$\langle x^{12} \rangle = \{e\}$$

This gives

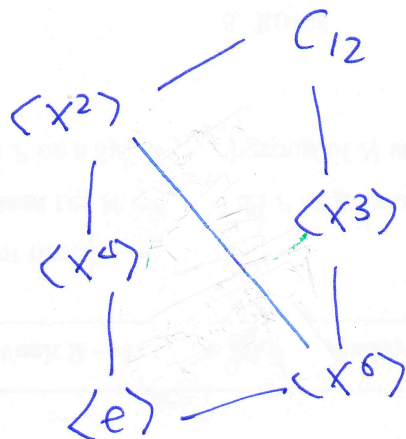


Usually we leave out "extra" edges as if

$H_1 \leq H_2 \leq H_3$  it is implied that

$H_1 \leq H_3$ . So we ~~don't draw~~ don't draw

an edge  
from  $H_1 - H_3$ .



Hence for  $C_{12}$  get

